

Prove each of the following trigonometric identities.

1.
$$\frac{\cos x}{1 - \sin x} - \sec x = \tan x$$

2.
$$\cos^4 x + 2 \cos^2 x \sin^2 x + \sin^4 x = 1$$

3.
$$\sin^4 x + \sin^2 x \cos^2 x = \sin^2 x$$

4.
$$(\sec x - \tan x)^2 = \frac{1 - \sin x}{1 + \sin x}$$

5.
$$\frac{\tan x}{\sec x} = \sin x$$

6.
$$\frac{\cos^2 x}{\sin x + 1} = 1 - \sin x$$

7.
$$\sin^4 x - \cos^4 x + \cos^2 x = \sin^2 x$$

8.
$$\frac{\cos^2 x - \sin^2 x}{\cos^2 x + \sin x \cos x} = 1 - \tan x$$